

CLOCKWORKING FLAVOR

ALONSO, AC, DILLON, KAMENIK, MARTIN - CAMALICH, ZUPAN JHEP 1810 2018 099 ARXIV:180709792

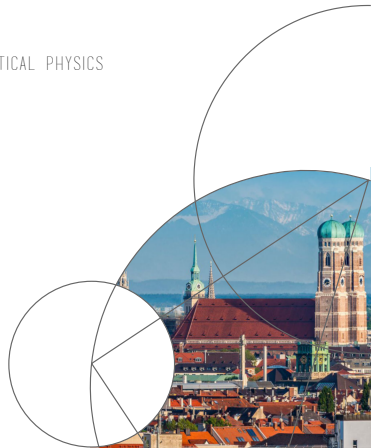
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PRISMA⁺

MIAPP WORKSHOP: FLAVOR 2019: NEW PHYSICS
IN FLAVOR FROM LHC TO BELLE II




A CLOCKWORK SOLUTION TO THE FLAVOR PUZZLE

$$\begin{pmatrix} \bar{q}_L^1 \\ \bar{q}_L^2 \\ \bar{q}_L^3 \end{pmatrix} \left(Y_U \right) \begin{pmatrix} u_R^1 \\ u_R^2 \\ u_R^3 \end{pmatrix} \quad \begin{pmatrix} \bar{q}_L^1 \\ \bar{q}_L^2 \\ \bar{q}_L^3 \end{pmatrix} \left(Y_D \right) \begin{pmatrix} d_R^1 \\ d_R^2 \\ d_R^3 \end{pmatrix}$$

THE CLOCKWORK MECHANISM

Generic mechanism to generate large hierarchies:

- in couplings Plot stolen from Kamenick's Planck 17


$$g_{\text{eff}} = g \times q^{-N}$$
$$\frac{1}{q} \times \frac{1}{q} \times \dots \times \frac{1}{q} \quad N - \text{times}$$

[Choi, Kim, Yun, '14]

[Choi, Im, '15]

[Kaplan, Rattazzi, '15]

[Giudice, McCullough, '15]

...

- in scales

$$\Lambda_{\text{eff}} = M/g_{\text{eff}}$$

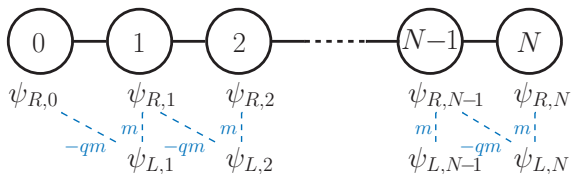
It is used to solve the **hierarchy problem** such

$$v_{\text{EW}} \sim M_{\text{Planck}} \times q^{-N}$$

In some cases, it can be viewed as the deconstructed version of the Linear Dilaton Model [Antoniadis, Arvanitaki, Dimopoulos, Giveon, '11][Baryakhtar, '12][Cox, Gherghetta, '12]

CLOCKWORKING A SINGLE FERMION

One chiral fermion $\psi_{R,0}$ plus N vector-like fermions ψ_k



$$\mathcal{L}_{\psi_R} = i \sum_{j=0}^N \bar{\psi}_{R,j} \not{D} \psi_{R,j} + i \sum_{j=1}^N \bar{\psi}_{L,j} \not{D} \psi_{L,j} - m \sum_{j=1}^N (\bar{\psi}_{L,j} \psi_{R,j} - q \bar{\psi}_{L,j} \psi_{R,j-1}) + \text{h.c.},$$

- We have $2N + 1$ chiral symmetries broken by $2N$ mass parameters $(q, mq) \Rightarrow$ We end up with a **massless chiral state**
- We assume all sites to share the same **gauge** group, i.e., \not{D} is not site dependent

CLOCKWORKING A SINGLE FERMION

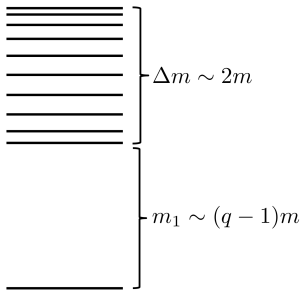
This pattern leads to a $N \times (N + 1)$ mass matrix,

$$\mathcal{M}_\psi = m \begin{pmatrix} -q & 1 & 0 & \dots & 0 \\ 0 & -q & 1 & \dots & 0 \\ \vdots & \ddots & \ddots & \ddots & 0 \\ 0 & \dots & 0 & -q & 1 \end{pmatrix},$$

which leads, after diagonalization, to a mass spectrum

$$M_k^2 = m^2 \left(1 + q^2 - 2q \cos \left(\frac{k\pi}{N+1} \right) \right)$$

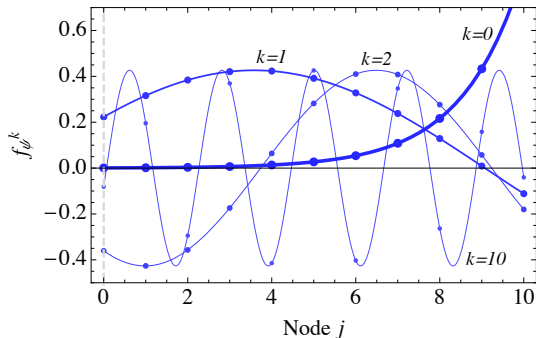
- Mass gap $M_1 \approx m(q - 1)$
- Mass splitting
 $M_N - M_1 \approx 2m$



CLOCKWORKING A SINGLE FERMION

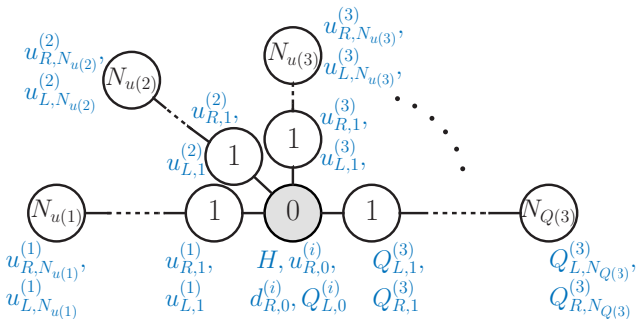
We are interested in the 0-site components f_{ψ}^k , i.e.,

$$\psi'_{R,k} = \sum_{j=0}^N V_{jk}^R \psi_{R,j}, \quad f_{\psi}^k = V_{0k}^R, \quad k = 0, \dots, N,$$



$$f_{\psi}^0 = \begin{cases} \sim 1/q^N, & q \gg 1; \\ \frac{1}{\sqrt{1+N}}, & q \rightarrow 1. \end{cases}$$

CLOCKWORK FLAVOR



- One clockwork chain per SM chiral fermion (q_{ψ_i}, N_{ψ_i}) , with the corresponding massless state identified with its SM counterpart
- The Higgs doublet lives in the 0-site

$$\bar{Q}_{L,0} Y_D H d_{R,0} + \bar{Q}_{L,0} Y_U \tilde{H} u_{R,0} + \text{h.c}$$

A CLOCKWORK MODEL OF FLAVOR

The SM-like Yukawas are given by

$$(Y_u^{\text{SM}})_{ij} = f_{Q(i)} (Y_U)_{ij} f_{u(j)} \sim q_{Q(i)}^{-N_{Q(i)}} (Y_U)_{ij} q_{u(j)}^{-N_{u(j)}}$$

$$(Y_d^{\text{SM}})_{ij} = f_{Q(i)} (Y_D)_{ij} f_{d(j)} \sim q_{Q(i)}^{-N_{Q(i)}} (Y_D)_{ij} q_{d(j)}^{-N_{d(j)}}$$

We can have hierarchical quark masses for $\mathcal{O}(1)$ proto-Yukawas if

$$\begin{aligned} q_{Q(1)}^{-N_{Q(1)}} &\ll q_{Q(2)}^{-N_{Q(2)}} \ll q_{Q(3)}^{-N_{Q(3)}} \\ q_{u(1)}^{-N_{u(1)}} &\ll q_{u(2)}^{-N_{u(2)}} \ll q_{u(3)}^{-N_{u(3)}} \\ q_{d(1)}^{-N_{d(1)}} &\ll q_{d(2)}^{-N_{d(2)}} \ll q_{d(3)}^{-N_{d(3)}} \end{aligned}$$

which leads to

$$\begin{aligned} \bar{m}_{u(i)} &\sim v f_{Q(i)} f_{u(i)} & \bar{m}_{d(i)} &\sim v f_{Q(i)} f_{d(i)} \\ |L_{u,d}|_{ij} &\sim f_{Q(i)}/f_{Q(j)} & |R_{u,d}|_{ij} &\sim f_{u,d(i)}/f_{u,d(j)} & (\mathbf{V}_{\text{CKM}})_{ij} &\sim f_{Q(i)}/f_{Q(j)} \end{aligned}$$

TWO LIMITS

There are two special limits

- ① The **universal q limit** (or the FN limit)

$$q \sim 1/\lambda \gg 1 \quad \text{fixed and} \quad N_{Q(1)} \gg N_{Q(2)} \gg N_{Q(3)}, \dots$$

- The total number of VLQs can be somehow reduced
- $q \sim 1/\lambda \gg 1 \Rightarrow M_k \sim qm$ **Compressed spectra**

- ② The **universal N limit** (or the RS limit)

$$N \gg 1 \quad \text{fixed and} \quad q_{Q(1)} \gg q_{Q(2)} \gg q_{Q(3)}, \dots$$

- A very large number of VLQs, $12 \times N$
- For the third generation $q \sim 1 \Rightarrow M_1 \approx m(q-1) \ll m$ **Light gears**

But we can find all kind of intermediate situations!

CW AS THE EFT OF SOME NEW FN

- The CW models of flavor do not contain a dynamical flavon
- The differences between the **universal- q CW** and the **FN models** will depend on the values of $m_{\text{arg}\phi}$ and $m_{\text{rad}\phi}$
- The **universal- q CW** can be seen as the low energy effective theory – for some range of the parameter space – of a different realization of **Froggatt-Nielsen** where $U(1)_H$ is non-anomalous and

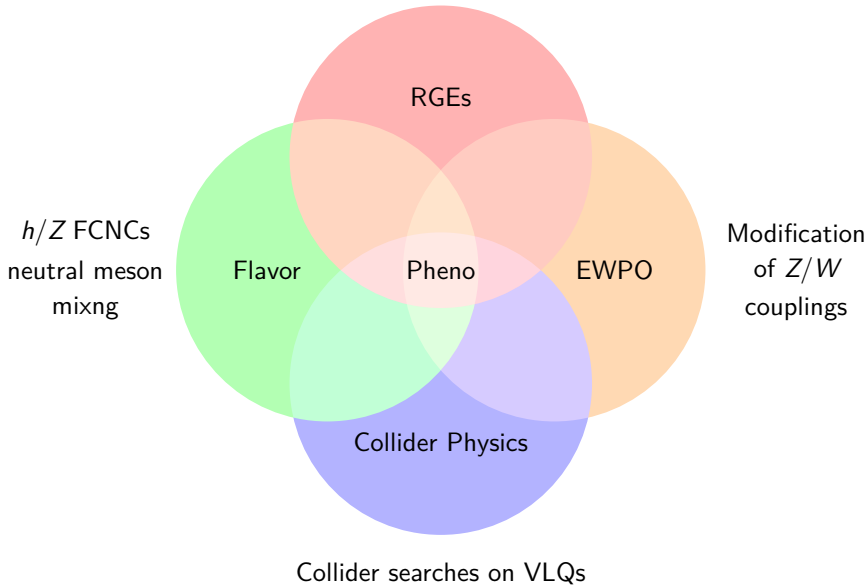
$$(Y_u^{\text{SM}})_{ij} \sim \left(\frac{\Lambda}{\langle \phi^* \rangle} \right)^{N_{Q(i)} + N_{u(j)}} \quad \text{CLOCKWORKED FN}$$

- If $U(1)_H$ is gauge, the new gauge boson have mass $m_H \sim g_H \langle \phi \rangle$ and mediate FNCNs $\Rightarrow m_H$ can be light enough if g_H is small [Zupan et al, soon]

PHENOMENOLOGY

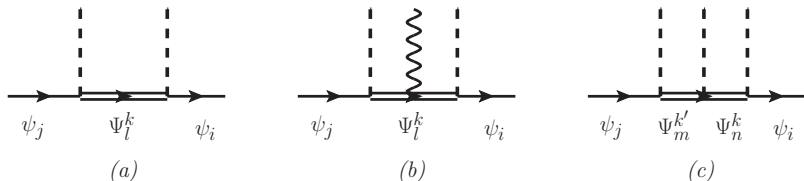
PHENOMENOLOGY

Modification of α_s and λ RGEs



LOW ENERGY CONSTRAINTS

All these light gears will mess up with flavor data and EWPO; at $\mathcal{O}(\frac{v^2}{M^2})$



However, there is some [Clockwork-GIM](#) mechanism helping with FCNCs. For instance, $Zd_{L(i)}d_L(j)$ receives corrections

$$[\delta g_L]_{ij}^{Z_d} = \frac{v^2}{4} f_{Q(i)} f_{Q(j)} \left[Y_D M_d^{-2} Y_D^\dagger \right]_{ij}$$

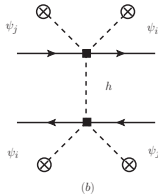
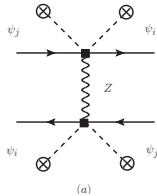
A strong constraint comes from $Z\bar{b}_L b_L$ since is not protected as $f_{Q(3)} = 1$

$$\Rightarrow M_{d(i)} \gtrsim 3.8 \text{ TeV}$$

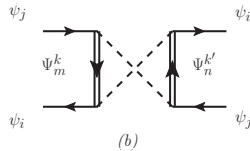
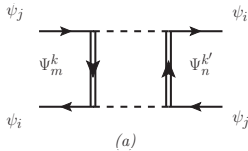
LOW ENERGY CONSTRAINTS

For neutral-meson mixing $K - \bar{K}$, $B - \bar{B}$, $D - \bar{D}$, ... we have

- Tree-level $\mathcal{O}(v^4/M^4)$ contributions



- One loop $\mathcal{O}(v^2/M^2)$ terms (finite pieces and mixing terms)



However, they still come with a large overlap suppression!

LOW ENERGY CONSTRAINTS

Assuming $q \sim 1/\lambda$ and $N_{\psi(i)}$ such

$$F_Q = \text{diag}(\lambda^3, \lambda^2, 1), \quad F_U = \text{diag}(\lambda^4, \lambda, 1), \quad F_D = \text{diag}(\lambda^4, \lambda^3, \lambda^2),$$

we obtain

$$\begin{array}{c} \bar{q}_L^1 \begin{array}{ccc} \text{gear} & \text{gear} & \text{gear} \end{array} \\ \bar{q}_L^2 \begin{array}{cc} \text{gear} & \text{gear} \end{array} \\ \bar{q}_L^3 \end{array} \left(Y_U \right) \begin{array}{c} \begin{array}{cccc} \text{gear} & \text{gear} & \text{gear} & \text{gear} \end{array} u_R^1 \\ \text{gear} u_R^2 \\ u_R^3 \end{array}$$

$$\begin{array}{c} \bar{q}_L^1 \begin{array}{ccc} \text{gear} & \text{gear} & \text{gear} \end{array} \\ \bar{q}_L^2 \begin{array}{cc} \text{gear} & \text{gear} \end{array} \\ \bar{q}_L^3 \end{array} \left(Y_D \right) \begin{array}{c} \begin{array}{cccc} \text{gear} & \text{gear} & \text{gear} & \text{gear} \end{array} d_R^1 \\ \begin{array}{ccc} \text{gear} & \text{gear} & \text{gear} \end{array} d_R^2 \\ \begin{array}{cc} \text{gear} & \text{gear} \end{array} d_R^3 \end{array}$$

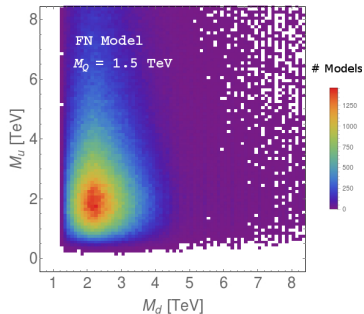
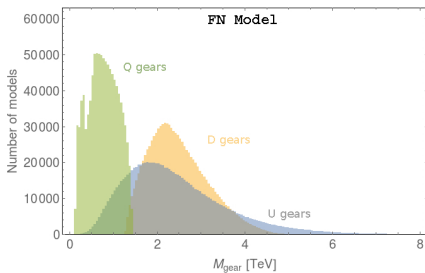
LOW ENERGY CONSTRAINTS

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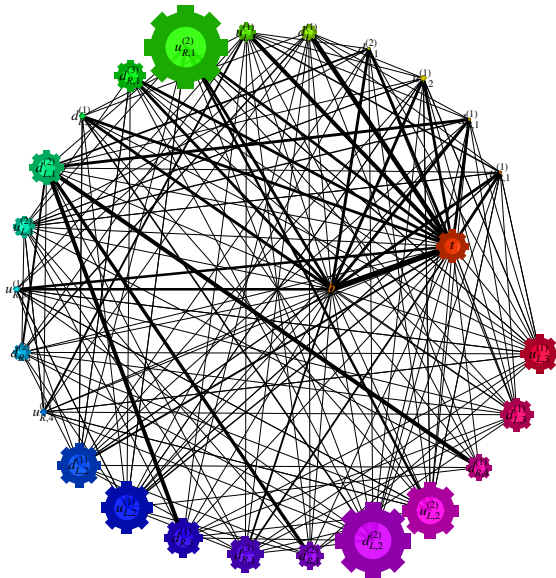
we obtain

Process	U	D	Q	UQ	DQ
$B_s - \bar{B}_s$	λ^4, \square^*	λ^4, \times and \square	λ^7, \square^*	λ^7, \square	λ^6, \times
$B - \bar{B}$	λ^6, \square^*	λ^6, \times and \square	λ^9, \square^*	λ^9, \square	λ^8, \times
$K - \bar{K}$	λ^{10}, \square^*	λ^{10}, \times and \square	$\lambda^{12}, \square^{*\dagger}$	$\lambda^{12}, \square^\dagger$	$\lambda^{12}, \times^\dagger$ and \square^\dagger
$D - \bar{D}$	λ^{10}, \times and \square	λ^{10}, \square	λ^{10}, \times and \square	$\lambda^8, \times^\dagger$	$\lambda^{10}, \square^\dagger$



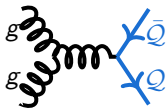
COLLIDER PHENO

Benchmark with $M_u \gtrsim 1.3$ TeV, $M_d \gtrsim 1.5$ TeV, $M_Q \gtrsim 1.7$ TeV

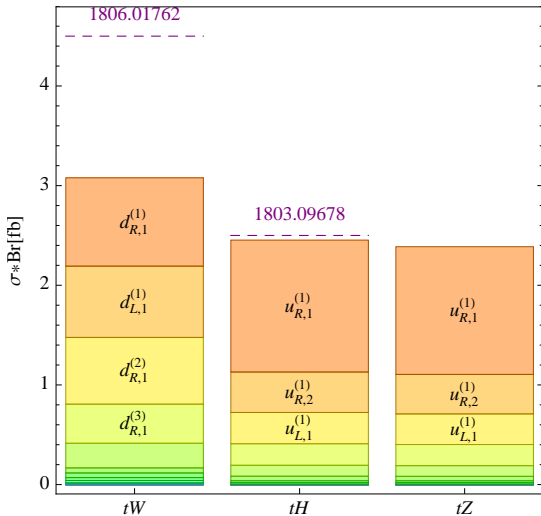


COLLIDER PHENO

TOP PARTNER SEARCHES

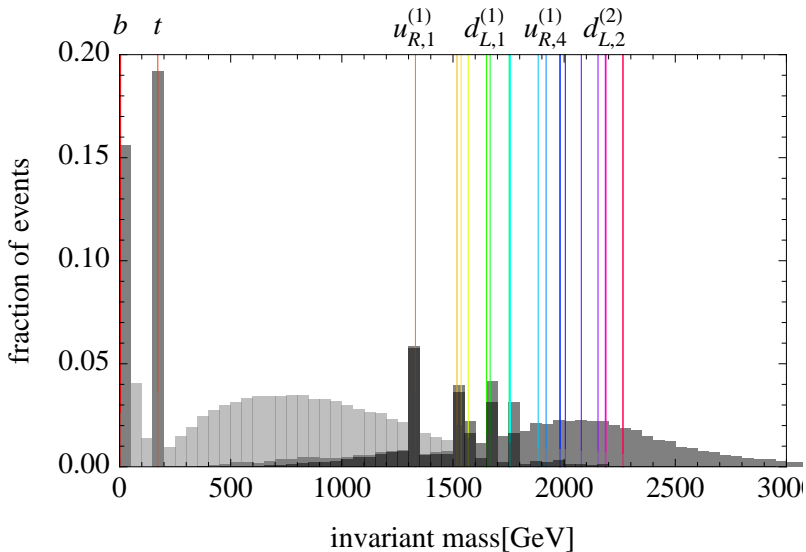


$$pp \rightarrow \bar{Q}Q \rightarrow \bar{Q} + tW/H/Z$$



COLLIDER PHENO

HEMISPHERE CLUSTERING



CONCLUSIONS

- The CW mechanism can also provide a rationale for the flavor puzzle
- There are two interesting limits, corresponding to universal values of q or N , which point to rather different UV completions
- The universal- q limit can be most easily matched to a different limit of the usual FN models, which we called [clockworked FN](#)
- These models are embedded with some [CW-GIM](#) flavor protection that allows to have very light gears
- We have put forward new ways of looking for such a peculiar fermion spectrum at colliders

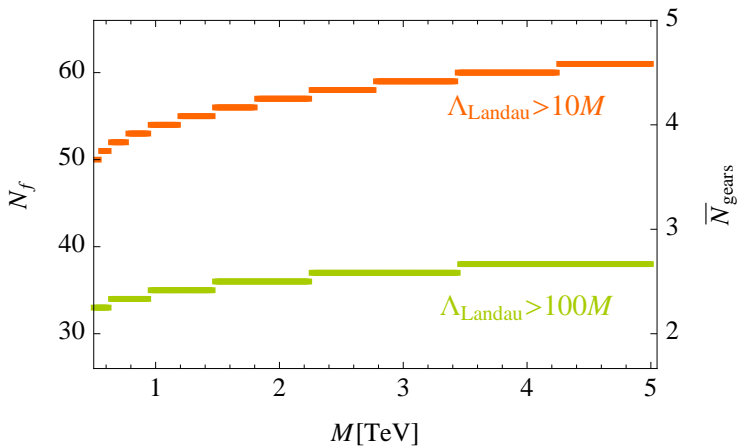
THANKS!

BACK - UP SLIDES

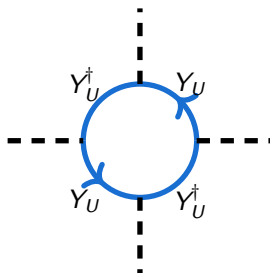
QCD LANDAU POLE

Having a bunch of heavy quarks will affect the running of α_s . Restricting ourselves to one loop,

$$\frac{d\alpha_s}{d\ln \mu} = -2\beta_0 \frac{\alpha_s^2}{4\pi}, \quad \beta_0 = \frac{11N_c - 2N_f}{3},$$



HIGGS QUARTIC COUPLING


$$\beta_\lambda \supset 12\text{Tr}\left(Y_U^\dagger Y_U\right) \lambda - 12\text{Tr}\left(Y_U Y_U^\dagger Y_U Y_U^\dagger\right)$$

β_λ receives very large contributions from sizable Yukawas!

Therefore, we should have Yukawa entries a bit smaller than 1 to have

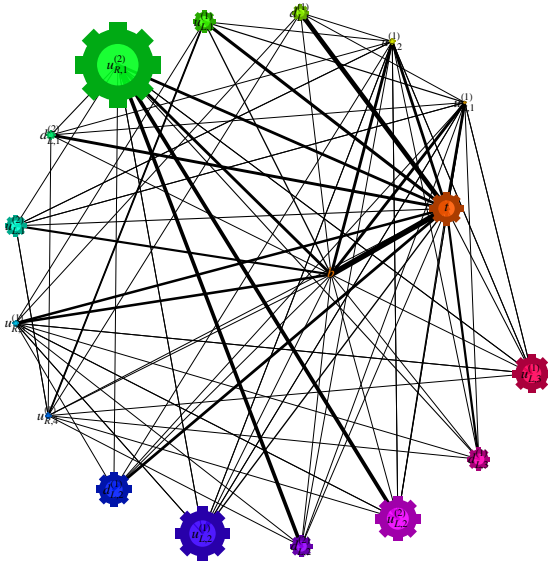
$$\text{Tr}\left(Y_U^\dagger Y_U Y_U^\dagger Y_U\right) + \text{Tr}\left(Y_D^\dagger Y_D Y_D^\dagger Y_D\right) \ll \frac{4\pi^2}{3}$$

This really disfavours the CW universal N limit since $y_t \sim (Y_U)_{33}/(1+N)$

However, one could add extra scalars or gauge bosons like e.g. [\[Sannino, Smirnov,](#)

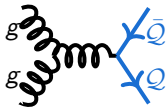
COLLIDER PHENO

Benchmark with $M_u \gtrsim 1.3$ TeV, $M_Q \gtrsim 1.7$ TeV, $M_d \gg M_{u,Q}$

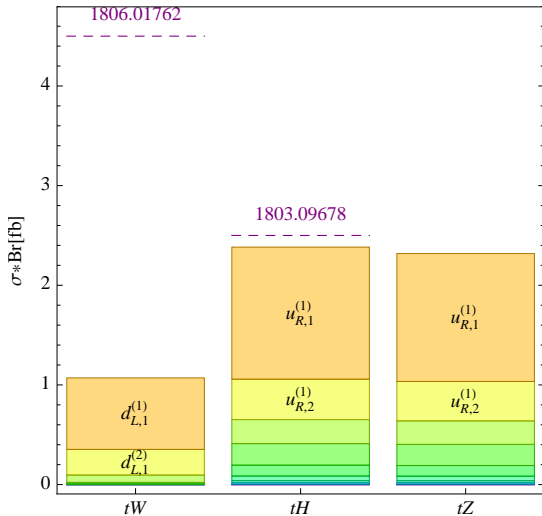


COLLIDER PHENO

TOP PARTNER SEARCHES



$$pp \rightarrow \bar{Q}Q \rightarrow \bar{Q} + tW/H/Z$$



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HEMISPHERE CLUSTERING

